## Lesson 6.5 The Amount and Present Value of an Annuity

Goal: Calculate the amount (future value) of a simple ordinary annuity Calculate the present value of a simple ordinary annuity

- An annuity is a series of equal payments paid in to our out of an account at regular intervals
- In an ordinary simple annuity, payments are made at the end of each compounding period
- The AMOUNT of an annuity (future value) is the sum of regular deposits plus interest


## Compound Periods (\# times per year)

> Annually: Semi-Annually:

Monthly: Semi-Monthly:
Weekly: Bi-weekly:
Quarterly: Daily:

The AMOUNT of an ordinary simple annuity is given by the formula $A=\frac{R\left[(1+i)^{n}-1\right]}{i}$, where
$A=\quad i=$
$R=$
$n=$

This formula can only be used when the payment interval is the same as the compounding period

Example Suppose $\$ 450$ were deposited at the end of each quarter for 1.5 years into an annuity that earns 10\% per year compounded quarterly
a) What is the amount of the annuity?
$A=$ ?
$R=$
$i=$
$n=$

The INTEREST of an ordinary simple annuity is given by the formula $\boldsymbol{I}=\boldsymbol{A}-\boldsymbol{R} \boldsymbol{n}$, where $\boldsymbol{I}$ is interest amount
b) How much interest did the annuity earn?

The present value of an annuity is the principal that must be invested TODAY to provide regular payments
The PRESENT VALUE of an ordinary simple annuity is given by the formula $P V=\frac{R\left[1-(1+i)^{-n}\right]}{i}$, where

$$
\begin{array}{ll}
P V= & i= \\
R= & n=
\end{array}
$$

This formula can only be used when the payment interval is the same as the compounding period

Example Victor wants to withdraw $\$ 700$ at the end of each month for 8 months, starting 1 month from now. His bank account earns $5.4 \%$ per year compounded monthly.
a) How much must Victor deposit in his account TODAY to pay for the withdrawals?
$P V=$ ?
$R=$
$i=$
$n=$

The INTEREST of an ordinary simple annuity is given by the formula $\boldsymbol{I}=\boldsymbol{R} \boldsymbol{n}-\boldsymbol{P} \boldsymbol{V}$, where $\boldsymbol{I}$ is interest
b) How much interest did the annuity earn?

