

Part 3: Exploring Reflections About the x-Axis:  $y = -f(x)$

A) Quadratic Function:  $y = x^2$

Complete the following tables of values and use them to graph and label each function.

x	$y = x^2$
-2	4
-1	1
0	0
1	1
2	4

x	$y = -x^2$
-2	-4
-1	-1
0	0
1	-1
2	-4

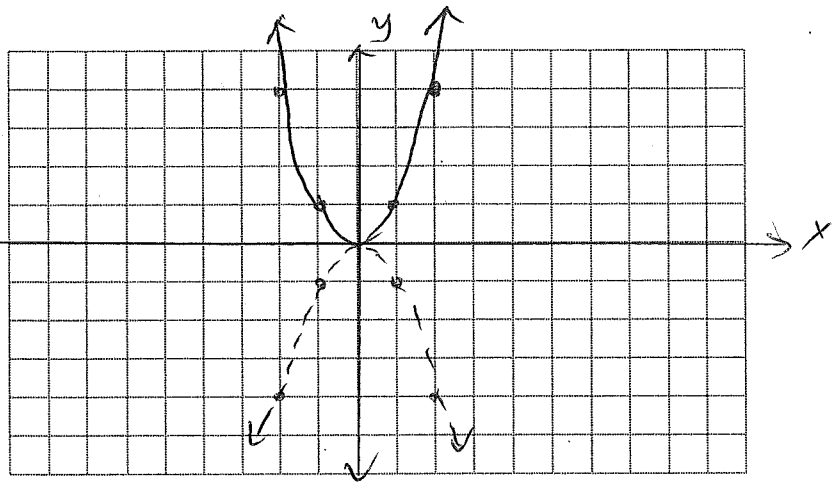
(a) ~

(b) ~

Compare the transformed function to the first function,  $y = x^2$ . Notice the similarities and differences of the coordinates of the points.

Reflection on x-axis.  
y-values are negated.

(0,0) is the invariant point.



B) Square Root Function:  $y = \sqrt{x}$

Complete the following tables of values and use them to graph and label each function.

x	$y = \sqrt{x}$
0	0
1	1
4	2
9	3
16	4

x	$y = -\sqrt{x}$
0	0
1	-1
4	-2
9	-3
16	-4

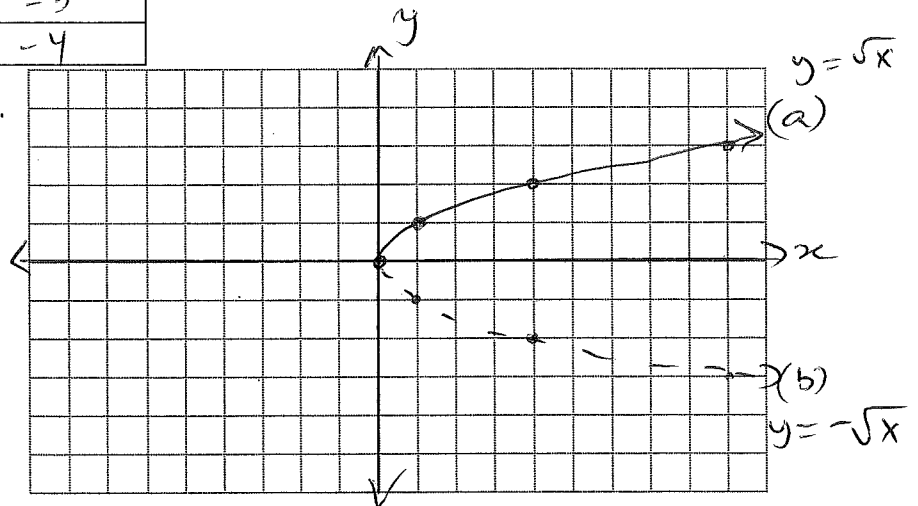
(a) ~

(b) ~

Compare the transformed function to the first function,  $y = \sqrt{x}$ . Notice the similarities and differences of the coordinates of the points.

Graph reflected around x-axis.

(0,0) invariant point  
y-values are negated.



C) Reciprocal Function:  $y = \frac{1}{x}$

Complete the following tables of values and use them to graph and label each function.

x	$y = \frac{1}{x}$
-4	-0.25
-1	-1
$-\frac{1}{4}$	-4
$\frac{1}{4}$	4
1	1
4	0.25

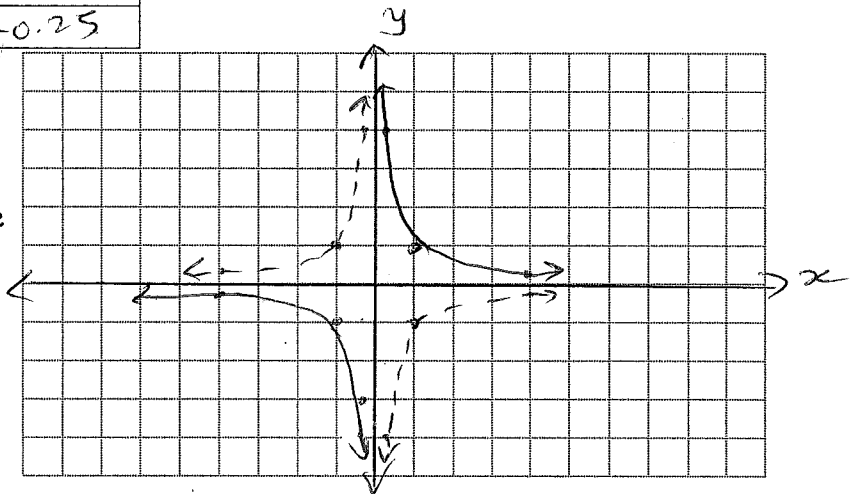
x	$y = -\frac{1}{x}$
-4	0.25
-1	1
$-\frac{1}{4}$	4
$\frac{1}{4}$	-4
1	-1
4	-0.25

(a) ~

(b) ~

Compare the transformed function to the first function,  $y = \frac{1}{x}$ . Notice the similarities and differences of the coordinates of the points.

- Reflection around x-axis
- No centroid point
- y-values are negated



SUMMARY

If  $y = f(x)$  is transformed to  $y = af(x)$ , describe the transformation:

1. If  $a = -1$ , then the graph will be reflected around x-axis
2. Any point  $(x, y)$  under this transformation becomes  $(x, -y)$ .

Part 4: Exploring Reflections About the y-Axis:  $y = f(-x)$

A) Quadratic Function:  $y = x^2$

Complete the following tables of values and use them to graph and label each function.

x	$y = x^2$
-2	4
-1	1
0	0
1	1
2	4

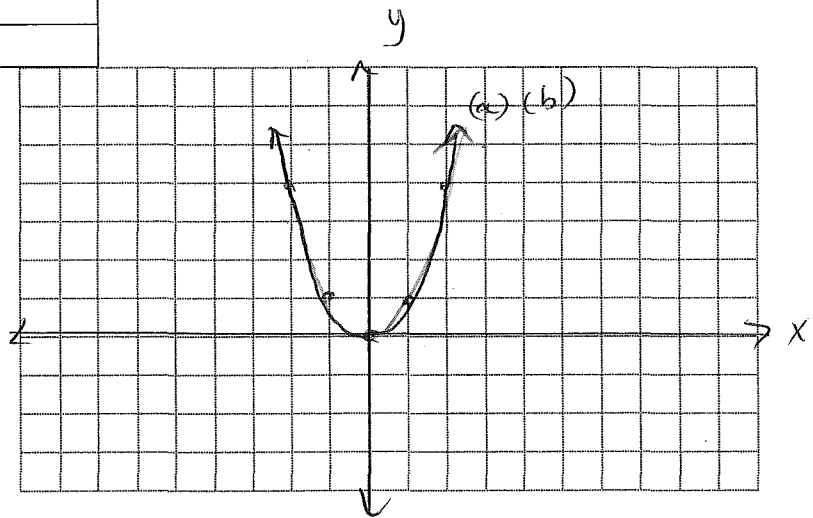
(a)

x	$y = (-x)^2$
2	4
1	1
0	0
-1	1
-2	4

(b)

Compare the transformed function to the first function,  $y = x^2$ . Notice the similarities and differences of the coordinates of the points.

Same parabola  
(Reflection in y-axis)



B) Square Root Function:  $y = \sqrt{x}$

Complete the following tables of values and use them to graph and label each function.

x	$y = \sqrt{x}$
0	0
1	1
4	2
9	3
16	4

(a)

x	$y = \sqrt{-x}$
0	0
-1	1
-4	2
-9	3
-16	4

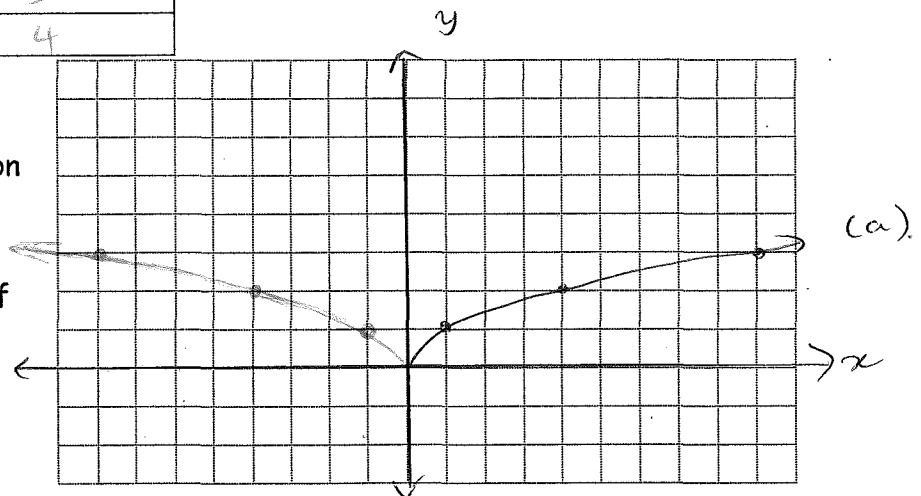
(b)

Compare the transformed function to the first function,  $y = \sqrt{x}$ . Notice the similarities and differences of the coordinates of the points.

↳ Reflection around y-axis.

↳ (0,0) invariant

↳ x-values are negated.



C) Reciprocal Function:  $y = \frac{1}{x}$

Complete the following tables of values and use them to graph and label each function.

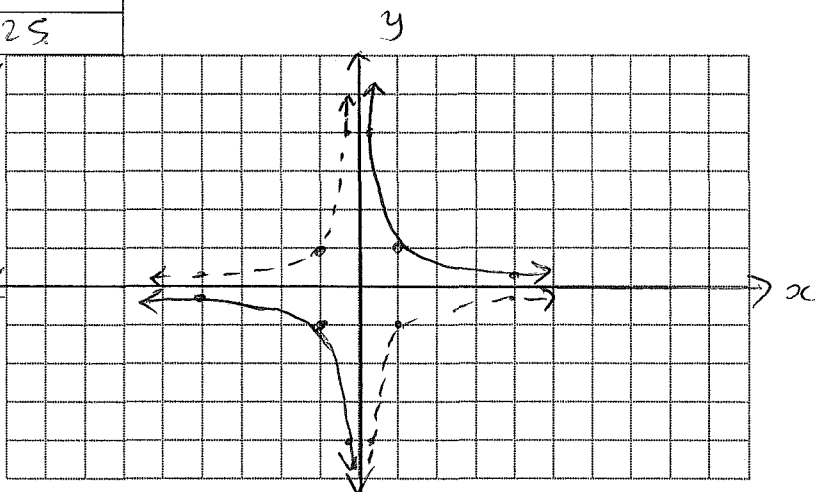
x	$y = \frac{1}{x}$
-4	-0.25
-1	-1
$-\frac{1}{4}$	-4
$\frac{1}{4}$	4
1	1
4	0.25

(a) ~

x	$y = \frac{1}{(-x)}$
4	-0.25
1	-1
$\frac{1}{4}$	-4
$-\frac{1}{4}$	4
-1	1
-4	0.25

(b) ~

Compare the transformed function to the first function,  $y = \frac{1}{x}$ . Notice the similarities and differences of the coordinates of the points.



SUMMARY

If  $y = f(x)$  is transformed to  $y = f(kx)$ , describe the transformation:

1. If  $k = -1$ , then the graph will be reflected around y-axis
2. Any point  $(x, y)$  under this transformation becomes  $(-x, y)$ .