

### Evaluating Expressions and Solving Equations

1. Write each expression as a single power, then evaluate:

$$a) 5^3 \times 5^5 = 5^8 = 390,625$$

$$b) \frac{6^9}{6^3 \times 6^2} = \frac{6^9}{6^5} = 6^4 = 1,296$$

$$c) 3^7 \times 9 \div 3^4 = 3^7 \cdot 3^2 \div 3^4 \\ = 3^9 \div 3^4 = 3^5 \\ = 243$$

$$d) (3^2)^3 \times (3^3)^0 = 3^6 \cdot 3^0 \\ = 3^6 (1) \\ = 729$$

2. Expand and simplify each of the following:

$$a) (16x^2 - 3x + 11) + (2 + x^2) \\ = 16x^2 + x^2 - 3x + 11 + 2 \\ = 17x^2 - 3x + 13$$

$$b) (4m - 3m^2) - (7m^2 - m) \\ = 4m - 3m^2 - 7m^2 + m \\ = -10m^2 + 5m$$

$$c) 3(x^2 + x) - 4(x^2 + 2x) \\ = 3x^2 + 3x - 4x^2 - 8x \\ = -x^2 - 5x$$

3. Solve for the unknown variable:

$$a) 5x - 4 = 21 \\ +4 \quad +4$$

$$5x = 25 \quad (\text{divide by } 5)$$

$$x = 5$$

$$b) 12 - 3y = 6 + 2y$$

$$-3y - 2y = 6 - 12$$

$$-5y = -6$$

$$y = \frac{6}{5}$$

$$c) \frac{x}{2} + \frac{1}{5} = 4x - \frac{1}{3} \quad (\text{multiply by } 30)$$

$$30\left(\frac{x}{2}\right) + 30\left(\frac{1}{5}\right) = 30(4x) - 30\left(\frac{1}{3}\right)$$

$$15x + 6 = 120x - 10$$

$$15x - 120x = -10 - 6 \\ -105x = -16 \Rightarrow x = \frac{16}{105}$$

$$d) \frac{1}{4}x + 3 = 2(2x + 1) \quad \text{multiply by } 4$$

$$4\left(\frac{1}{4}x\right) + 4(3) = 8(2x + 1)$$

$$x + 12 = 16x + 8$$

$$x - 16x = 8 - 12$$

$$-15x = -4 \Rightarrow x = \frac{4}{15}$$

4. Evaluate each expression where  $a = -2$ .

$$a) 8 - 5a$$

$$= 8 - 5(-2)$$

$$= 8 + 10$$

$$= 18$$

$$b) -a^2 + a + 2$$

$$= -(-2)^2 + (-2) + 2$$

$$= -4 + (-2) + 2$$

$$= -4$$

$$c) \frac{3a-2}{a}$$

$$= \frac{3(-2) - 2}{-2}$$

$$= \frac{-6 - 2}{-2}$$

$$= \frac{-8}{-2} = 4$$

5. Evaluate each expression where  $c = -4$  and  $d = -3$ .

a)  $-2cd$

$$= -2(-4)(-3)$$

$$= -24$$

b)  $2c - 2d$

$$= 2(-4) - 2(-3)$$

$$= -8 + 6$$

$$= -2$$

c)  $(c + 3d)^2$

$$= (-4 + 3(-3))^2$$

$$= (-4 - 9)^2$$

$$= (-13)^2$$

$$= 169$$

d)  $2d^2 - 3c + 5$

$$= 2(-3)^2 - 3(-4) + 5$$

$$= 2(9) + 12 + 5$$

$$= 18 + 12 + 5$$

$$= 35$$

e)  $(c - 2)(8 + d)$

$$= (-4 - 2)(8 - 3)$$

$$= (-6)(5)$$

$$= -30$$

6. Solve the following equations algebraically. Be sure to show all your work. Answers should be expressed as fractions in lowest terms, if necessary.

a)  $6p + 5 = 23$

$$\quad -5 \quad -5$$

$$6p = 18$$

$$p = \frac{18}{6}$$

$$p = 3$$

b)  $5x + 14 - 3x = 4x + 20$

$$2x + 14 = 4x + 20$$

$$2x - 4x = 20 - 14$$

$$-2x = 6$$

$$x = \frac{6}{-2}$$

$$x = -3$$

c)  $5(2x - 1) - 7 = 3(1 - 2x) + 17$

$$10x - 5 - 7 = 3 - 6x + 17$$

$$10x - 12 = -6x + 20$$

$$10x + 6x = 20 + 12$$

$$16x = 32$$

$$x = 2$$

d)  $\frac{x-3}{2} = \frac{x+1}{4} + 3$  (multiply by 4)

$$4\left(\frac{x-3}{2}\right) = 4\left(\frac{x+1}{4}\right) + 4(3)$$

$$2(x-3) = x+1+12$$

$$2x-6 = x+13$$

$$2x-x = 13+6$$

$$x = 19$$

e) Verify your solution to question 6b. Show your work below.

LS	RS
$5x + 14 - 3x$	$4x + 20$
$5(-3) + 14 - 3(-3)$	$4(-3) + 20$
$-15 + 14 + 9$	$-12 + 20$
8	8

$$LS = RS$$

$$\therefore x = -3$$

Evaluating Algebraic Expressions

1. Find the value of each expression if  $a = -2$  and  $b = 3$ .

a)  $a + b$   
 $= -2 + 3$   
 $= 1$

b)  $a - 2b$   
 $= -2 - 2(3)$   
 $= -2 - 6$   
 $= -8$

c)  $\frac{1}{2}a - \frac{1}{3}b$   
 $= \frac{1}{2}(-2) - \frac{1}{3}(3)$   
 $= -1 - 1$   
 $= -2$

2. Simplify.

a)  $(2x - 5) + (8x + 13)$   
 $= 2x + 8x - 5 + 13$   
 $= 10x + 8$

b)  $(5a - 7ab) + (6b + 4a) - (9ab - 3a + 3b)$   
 $= 5a - 7ab + 6b + 4a - 9ab + 3a - 3b$   
 $= -16ab + 12a + 3b$

c)  $-2(4x + 5y) + 4(8x - 7y)$   
 $= -8x - 10y + 32x - 28y$   
 $= 24x - 38y$

d)  $-7(x^2 + 6x + 9) - 5(2x^2 - 3x + 4)$   
 $= -7x^2 - 42x - 63 - 10x^2 + 15x - 20$   
 $= -17x^2 - 27x - 83$

Solving Equations

3. Solve.

a)  $3y + 5 = 11$   
 $-5 \quad -5$   
 $3y = 6$   
 $y = 2$

b)  $4x - 3 = -11$   
 $+3 \quad +3$   
 $4x = -8$   
 $x = -2$

c)  $17 = 4c - 3$   
 $+3 \quad +3$   
 $20 = 4c$   
 $c = \frac{20}{4} = 5$

d)  $6x + 8 = 4x - 10$   
 $6x - 4x = -10 - 8$   
 $2x = -18$   
 $x = -9$

e)  $9p - 10 = 6 + p$   
 $9p - p = 6 + 10$   
 $8p = 16$   
 $p = 2$

f)  $2m + 6.1 = 16.5$   
 $2m = 16.5 - 6.1$   
 $2m = 10.4$   
 $m = 5.2$

g)  $\frac{x}{2} = 4$   
 $x = 4(2)$   
 $= 8$

h)  $\frac{3x}{5} = -9$   
 $3x = -45$   
 $x = -15$

i)  $6 = \frac{m}{4}$   
 $m = (6)(4)$   
 $= 24$

j)  $2\frac{x}{-7} = 6$   
 $2x = -42$   
 $x = \frac{-42}{2}$   
 $= -21$

k)  $3 = \frac{3}{2}x - 3$   
 $+3 \quad +3$   
 $6 = \frac{3}{2}x$   
 $3x = 12$   
 $x = 4$

l)  $\frac{1}{4}x - 3 = 5$   
 $+3 \quad +3$   
 $\frac{1}{4}x = 8$   
 $x = 32$

A linear relationship can be written in the standard form  $Ax + By + C = 0$  and slope y-intercept form  $y = mx + b$

Graph:  $2x - y - 1 = 0$

**METHOD 1: SLOPE and Y-INTERCEPT**

**Step 1:** Rearrange the equation in slope y-intercept form as  $y = mx + b$

$2x - y - 1 = 0$   
 $+y$      $+y$

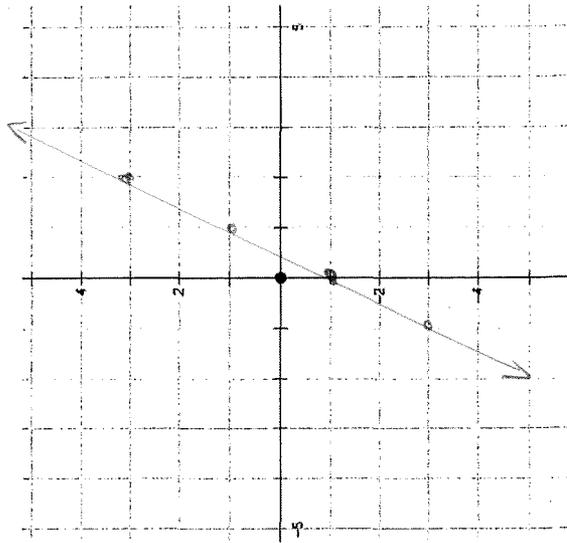
$y = 2x - 1$

**Step 2:** Determine the slope (m) and y-intercept (b)

**Slope (m) = 2 and y-intercept (b) = -1**

$2 = \frac{2}{1}$  1 right 2 up. or 1 left 2 down

**Step 3:** Plot the y-intercept first. From there, move right (always) as much as run, then move up if slope + or down if slope - to find a second point and connect with an extended line.



**METHOD 2: USING X AND Y - INTERCEPTS**

**Step 1:** To find the x-intercept, let  $y = 0$  and solve for x.

$2x - y - 1 = 0$  (sub  $y = 0$ )

$2x - 0 - 1 = 0$

$2x = 1$

$x = \frac{1}{2}$      $\therefore$  x-int is  $\frac{1}{2}$

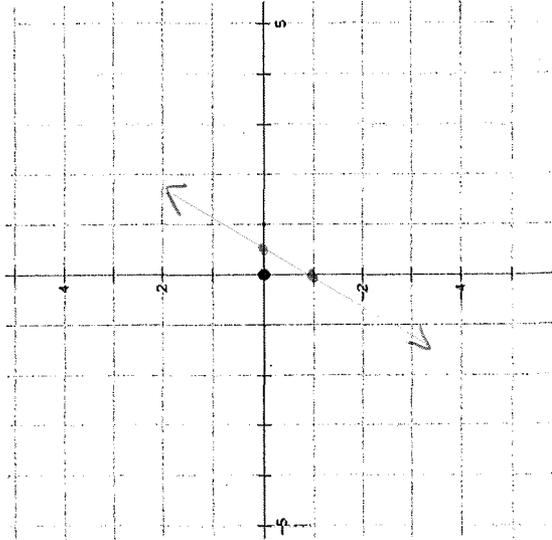
**Step 2:** To find the y-intercept, let  $x = 0$  and solve for y.

$2x - y - 1 = 0$  (sub  $x = 0$ )

$2(0) - y - 1 = 0$

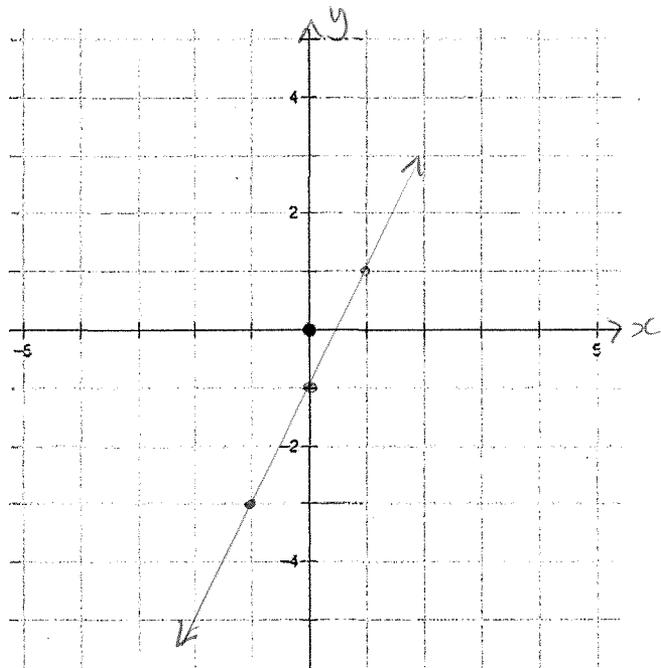
$-y - 1 = 0$

$y = -1$      $\therefore$  y-int is  $-1$ .



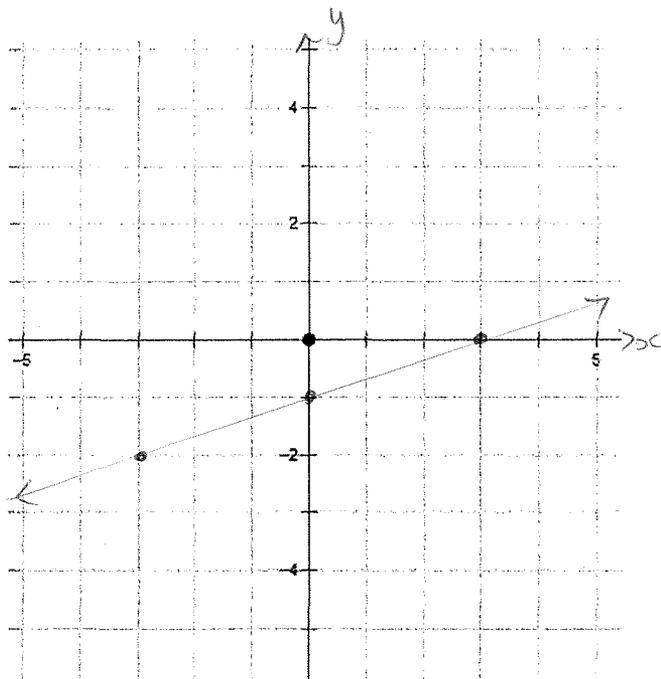
**METHOD 3: TABLE OF VALUES ( $y=mx+b$ )**

X	Y = $2x - 1$	POINTS
-1	$= 2(-1) - 1$ $= -2 - 1$ $= -3$	A(-1, -3)
0	$= 2(0) - 1$ $= 0 - 1$ $= -1$	B(0, -1)
1	$= 2(1) - 1$ $= 2 - 1$ $= 1$	C(1, 1)



Ex2. Graph  $y = \frac{1}{3}x - 1$  using a table of values. (select  $x$ -values that are multiple of 3)

$x$	$y$
-3	$\frac{1}{3}(-3) - 1$ $= -1 - 1$ $= -2$
0	$\frac{1}{3}(0) - 1$ $= 0 - 1$ $= -1$
3	$\frac{1}{3}(3) - 1$ $= 1 - 1$ $= 0$



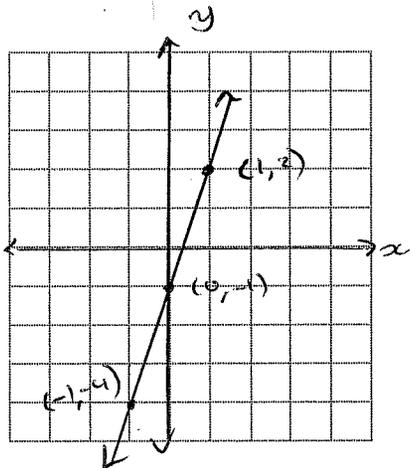
PRACTICE

Graphing

1. Graph each equation using a table of values

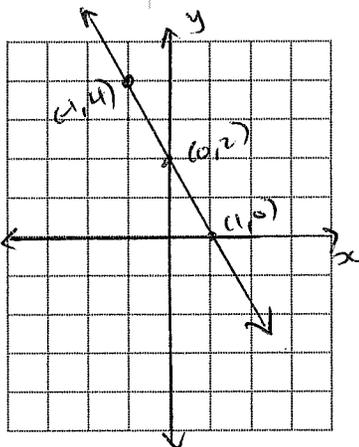
a)  $y = 3x - 1$

x	y
-1	-4
0	-1
1	2



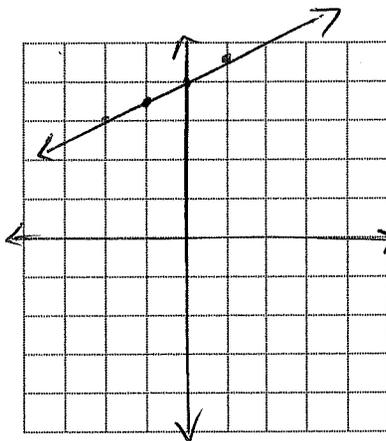
b)  $y = -2x + 2$

x	y
-1	4
0	2
1	0



c)  $y = \frac{1}{2}x + 4$

x	y
-1	3.5
0	4
1	4.5

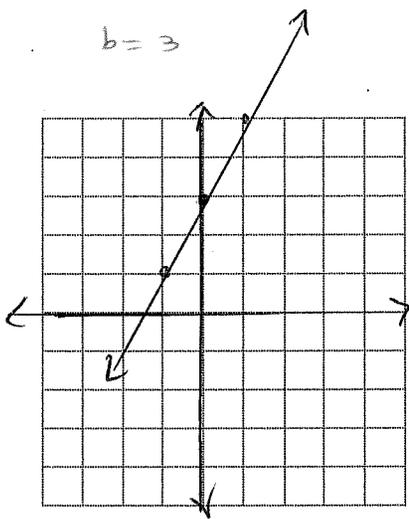


2. Graph each equation using the slope and y-intercept.

a)  $y = 2x + 3$

$m = 2$

$b = 3$



$m = 2$

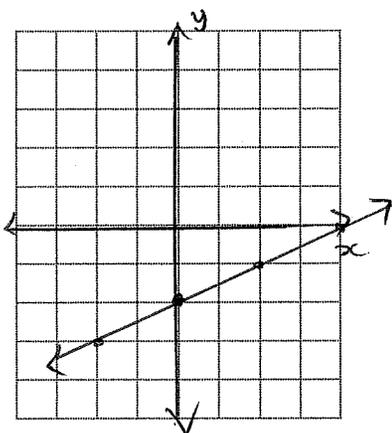
↑ R UP

OR IL 2D

b)  $y = \frac{1}{2}x - 2$

$m = \frac{1}{2}$

$b = -2$



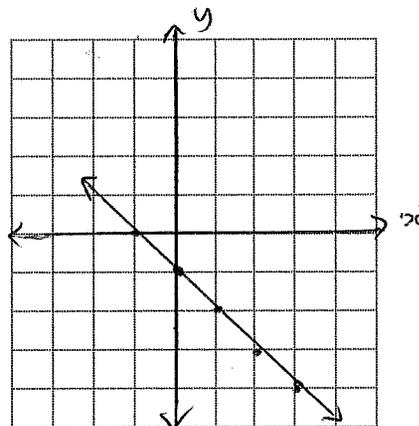
$m = \frac{1}{2}$

2R 1U

c)  $x + y + 1 = 0 \Rightarrow y = -x - 1$

$m = -1$

$b = -1$



$m = -1$

∴ 1R 1D

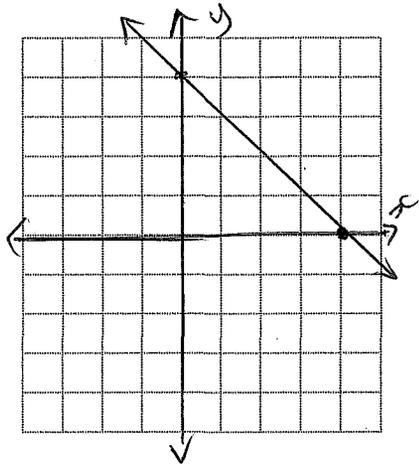
OR IL 1U

3. Graph each equation by determining the intercepts.

a)  $x + y = 4$

$x$ -int: set  $y=0$   
 $x = 4$

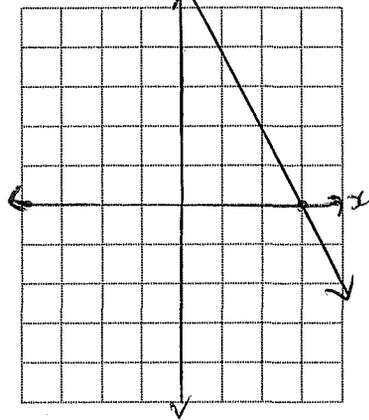
$y$ -int: set  $x=0$   
 $y = 4$



b)  $2x + y = 6$

$x$ -int: set  $y=0$   
 $2x = 6$   
 $x = 3$

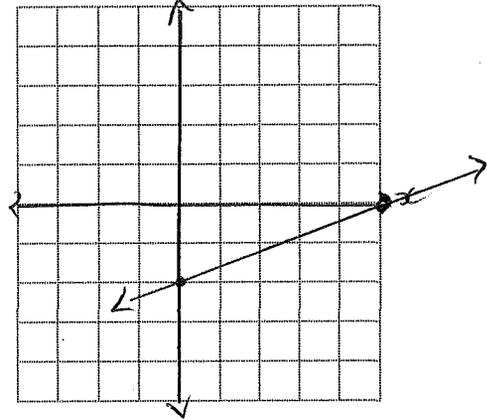
$y$ -int: set  $x=0$   
 $y = 6$



c)  $2x - 5y = 10$

$x$ -int: set  $y=0$   
 $2x = 10$   
 $x = 5$

$y$ -int: set  $x=0$   
 $-5y = 10$   
 $y = -2$

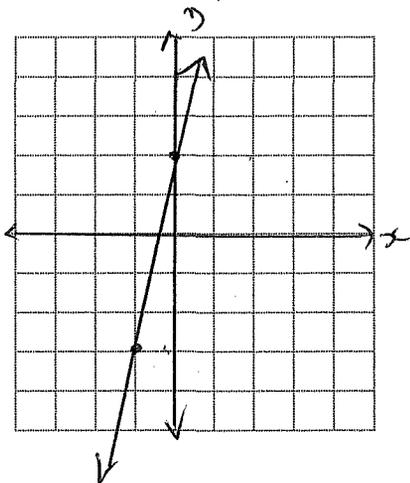


4. Graph each equation using the most suitable method.

a)  $y = 5x + 2$

$m = 5$

$b = 2$

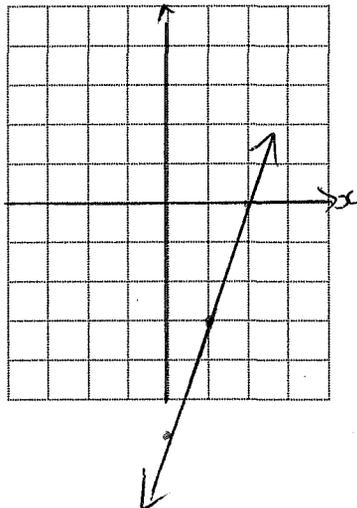


b)  $3x - y = 6$

$y = 3x - 6$

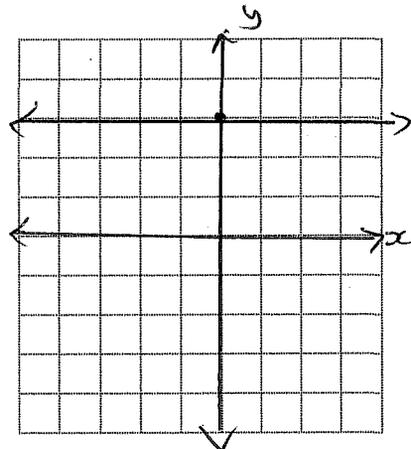
$m = 3$

$b = -6$



c)  $y = 3$

horizontal line



$$\text{slope} = \frac{\text{rise}}{\text{run}}; \text{slope} = \frac{y_2 - y_1}{x_2 - x_1}; \text{slope} = \frac{\Delta y}{\Delta x}; y\text{-intercept} = (0, b); y = mx + b$$

1. Determine the equation of the line with a slope of  $\frac{3}{2}$  and passes through the point  $(-3, 7)$ .

$$y = m(x - x_1) + y_1$$

$$y = \frac{3}{2}(x + 3) + 7$$

$$= \frac{3}{2}x + \frac{9}{2} + 7$$

$$= \frac{3}{2}x + \frac{9}{2} + \frac{14}{2}$$

$$\therefore y = \frac{3}{2}x + \frac{23}{2}$$

2. Determine the equation of the line that passes through the points

a.  $(4, -1)$  and  $(7, 8)$ .

b.  $(-3, -5)$  and  $(2, -3)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - (-1)}{7 - 4} = \frac{9}{3} = 3$$

$$m = \frac{-3 - (-5)}{2 - (-3)} = \frac{2}{5}$$

$$y = m(x - x_1) + y_1$$

$$y = m(x - x_1) + y_1$$

$$y = 3(x - 7) + 8$$

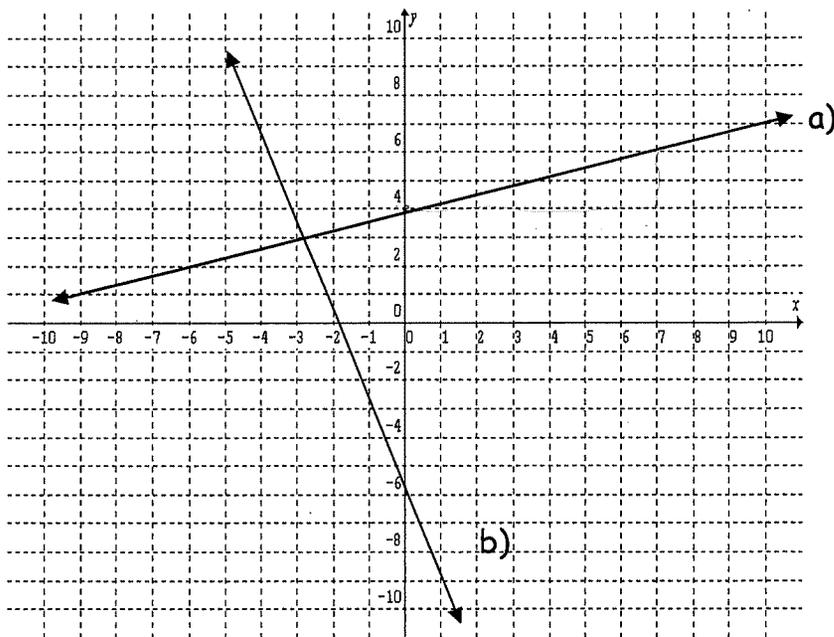
$$= 3x - 21 + 8$$

$$= 3x - 13$$

$$= \frac{2}{5}(x + 3) - 5$$

$$= \frac{2}{5}x + \frac{6}{5} - 5 = \frac{2}{5}x - \frac{19}{5}$$

3. Determine the equation of the following lines.



$$a) m = \frac{2}{7}$$

$$b = 4$$

$$\therefore y = \frac{2}{7}x + 4$$

$$b) m = -\frac{3}{1}$$

$$b = -6$$

$$\therefore y = -3x - 6$$

## Rules for Standard Form (Another way to write the equation of a line!)

- Must be in the form  $Ax + By + C = 0$  where A and B cannot both be zero.
- A must be a whole number (no leading negatives!)
- B, C must be integers.
- A, B, C must not have any factors common to all (can't all be divided by the same number)

Examples: Convert the following equations into standard form.

<p>a. <math>y = -3x + 2</math>  <math>3x + y - 2 = 0</math></p>	<p>b. <math>y = 2x + 1</math>  <math>-y - 2x - 1 = 0</math>  <math>2x - y + 1 = 0</math></p>
<p>c. <math>y = \frac{3}{5}x - 5</math> (multiply by 5)  <math>5y = 3x - 25</math>  <math>3x - 5y - 25 = 0</math></p>	<p>d. <math>-3y = 2.5x + 1</math> (multiply by 2)  <math>-6y = 5x + 2</math>  <math>5x + 6y + 2 = 0</math></p>
<p>e. <math>y = \frac{1}{2}x - \frac{2}{3}</math> (multiply by 6)  <math>6y = 3x - 4</math>  <math>3x - 6y - 4 = 0</math></p>	<p>f. <math>y = -5x + \frac{1}{3}</math> (multiply by 3)  <math>3y = -15x + 1</math>  <math>15x + 3y - 1 = 0</math></p>
<p>g. <math>y + 3x = -5x + 7y - 1</math>  <math>y + 3x + 5x - 7y + 1 = 0</math>  <math>8x - 6y + 1 = 0</math></p>	<p>h. <math>-3y = 6x + 18</math>  <math>+3y + 3y</math>  <math>6x + 3y + 18 = 0</math> (Reduce, <math>\div</math> by 3)  <math>2x + y + 6 = 0</math></p>

**Extra Practice: Write the equation for the following (in standard form where possible):**

a. slope of 4 and passing through (0, 7)

$$y = 4x + 7$$

↓  
y-int

b. horizontal and passing through the point (-5, 18)

horizontal line  $\Rightarrow m = 0$   
 $\therefore y = \#$

$y = 18$  is the equation.

c.  $m = \frac{9}{2}$  and passing through (-1, 4)

$$y = m(x - x_1) + y_1$$

$$= \frac{9}{2}(x + 1) + 4$$

$$= \frac{9}{2}x + \frac{9}{2} + \frac{8}{2}$$

$$= \frac{9x}{2} + \frac{17}{2}$$

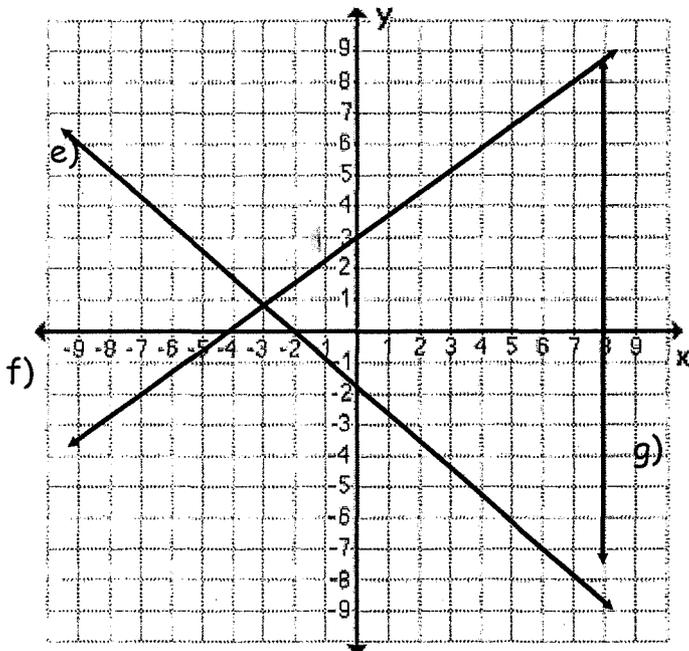
d. passing through the points (-3, 7) and (2, 4)

$$m = \frac{4 - 7}{2 - (-3)} = \frac{-3}{5}$$

$$y = m(x - x_1) + y_1$$

$$= \frac{-3}{5}(x - 2) + 4$$

$$= \frac{-3}{5}x + \frac{6}{5} + 4 = \frac{-3}{5}x + \frac{26}{5}$$



e)  $y = -x - 2$

f)  $y = \frac{2}{3}x + 3$

g)  $x = 8$