

Working with Polynomials

1. Simplify.

a) $(x^2 - 3x + 5) - (2x^2 - 5x - 7)$

$$= x^2 - 3x + 5 - 2x^2 + 5x + 7$$

$$= -x^2 + 2x + 12$$

$$(2x-3)^2 = (2x-3)(2x-3)$$

$$= 4x^2 - 6x - 6x + 9$$

$$= 4x^2 - 12x + 9$$

b) $x(2x-3)^2 - 2x(x-4)$

$$= x(4x^2 - 12x + 9) - 2x^2 + 8x$$

$$= 4x^3 - 12x^2 + 9x - 2x^2 + 8x$$

$$= 4x^3 - 14x^2 + 17x$$

2. Simplify. Hint: work inside out (do inside brackets first, then bigger outside brackets).

a) $4[2x - (3 - 5x)] + 3[3x - (4 + x)]$

$$= 4[2x - 3 + 5x] + 3[3x - 4 - x]$$

$$= 4[7x - 3] + 3[2x - 4]$$

$$= 28x - 12 + 6x - 12$$

$$= 34x - 24$$

b) $5[x - (2x + 3)] - 2[4x - (x + 1)]$

$$= 5[x - 2x - 3] - 2[4x - x - 1]$$

$$= 5[-x - 3] - 2[3x - 1]$$

$$= -5x - 15 - 6x + 2$$

$$= -11x - 13$$

3. Simplify.

a) $(x+2)(x^2 - x - 2)$

$$= x^3 - x^2 - 2x + 2x^2 - 2x - 4$$

$$= x^3 + x^2 - 4x - 4$$

b) $(1-x)(x^3 - x^2 + 3x)$

$$= x^3 - x^2 + 3x - x^4 + x^3 - 3x^2$$

$$= -x^4 + 2x^3 - 4x^2 + 3x$$

c) $(2 - x^2)(3 + x^2 - x^3)$

$$= 6 + 2x^2 - 2x^3 - 3x^2 - x^4 + x^5$$

$$= x^5 - x^4 - 2x^3 - x^2 + 6$$

d) $(x^2 + 1)(x^2 - 3x + 5)$

$$= x^4 - 3x^3 + 5x^2 + x^2 - 3x + 5$$

$$= x^4 - 3x^3 + 6x^2 - 3x + 5$$

Solutions:

1. a) $-x^2 + 2x + 12$ b) $4x^3 - 14x^2 + 17x$
 3. a) $x^3 + x^2 - 4x - 4$ b) $-x^4 + 2x^3 - 4x^2 + 3x$

2. a) $34x - 24$ b) $-11x - 13$
 c) $x^5 - x^4 - 2x^3 - x^2 + 6$ d) $x^4 - 3x^3 + 6x^2 - 3x + 5$

4. Simplify.

a) $(x+3)(x-1) - (x-5)(x-2)$

$$\begin{aligned}
 &= x^2 - x + 3x - 3 - [x^2 - 2x - 5x + 10] \\
 &= x^2 - x^2 + 2x + 9x - 3 - 10 \\
 &= 9x - 13
 \end{aligned}$$

b) $(2x^2 - 1)^2 - (4 - x^2)^2$

$$\begin{aligned}
 &= (2x^2 - 1)(2x^2 - 1) - [(4 - x^2)(4 - x^2)] \\
 &= 4x^4 - 2x^2 - 2x^2 + 1 - [16 - 4x^2 - 4x^2 + x^4] \\
 &= 4x^4 - x^4 - 4x^2 + 8x^2 + 1 - 16 \\
 &= 3x^4 + 4x^2 - 15.
 \end{aligned}$$

5. Simplify.

a) $(x-1)(x+3)(x+1) + (2x-1)(x-2)$

$$\begin{aligned}
 &= (x-1)[x^2 + 3x + 3] + 2x^2 - 4x - x + 2 \\
 &= (x-1)(x^2 + 4x + 3) + 2x^2 - 5x + 2 \\
 &= x^3 + \underline{4x^2 + 3x} - \underline{x^2 + 4x + 3} + \underline{2x^2 - 5x + 2} \\
 &= x^3 + 5x^2 - 6x - 1
 \end{aligned}$$

b) $(2a+7)^2(a-2) + 2(a^2 - 1)(4a + 3)$

6. Jake wrote the following: $(x+1)^2 - (x+2)(x-3) = x^2 + 2x + 1 - x^2 - x - 6$
 $= x - 5$

What mistake(s) did he make? Write a correct simplification, and explain how to avoid making Jake's error.

Brackets are needed around $(x+2)(x-3)$.7. If $x + y + z = 1$ and $x^2 + y^2 + z^2 = 3$, find the value of $xy + xz + yz$.

$(x+y+z)^2 = 1$

$(x+y+z)(x+y+z) = 1$

$\cancel{(x^2 + xy + xz + yx + yz + z^2)} + 2xz + 2yz + 2z^2 = 1$

$x^2 + y^2 + z^2 + 2xy + 2xz + 2yz = 1$

Solutions:

4. a) $9x - 13$ b) $3x^4 + 4x^2 - 15$ 5. a) $x^3 + 5x^2 - 6x - 1$ b) $12a^3 + 26a^2 - 15a - 104$

6. Jake did not subtract the last 2 terms. The correct answer is $3x + 7$. Avoid this error by using brackets. 7. -1

Homework: p. 88 # (4-6)ef, 10-12, 17a

p. 95 #2,4ef,5e,8-10,13,14a

Nelson, Mathematics 11 pp. 375-376

$$\begin{aligned}
 3 + 2(xy + xz + yz) &= 1 \\
 2(xy + xz + yz) &= -2 \\
 xy + xz + yz &= -1
 \end{aligned}$$
