

THE METHOD OF SUBSTITUTION

1. Choose an equation and **isolate** one variable (* pick the easiest one!).
2. Substitute one equation into the other (Sub ① in ②).
3. Solve the new equation for the other variable.
4. Substitute that result ($x = \#$) into one of the original equations.
5. Check your solution in both original equations.

Example 1

Solve the linear system using the method of substitution.

- ① $y = 2x + 4$
- ② $3x + y = 9$

Sub what represents y in equation ① into where you see " y " in equation ②

Step 1

$$\text{① } y = 2x + 4$$

$$\text{② } 3x + y = 9 \quad \text{replace "y" with } 2x + 4$$

Step 2

$$3x + 2x + 4 = 9$$

$$5x + 4 = 9$$

$$5x = 5$$

$$x = 1$$

Step 3

Sub "1" for "x" in equation ①

$$\text{① } y = 2x + 4$$

$$y = 2(1) + 4$$

$$y = 6$$

\therefore P.O.I. = (1, 6)

CHECK	
$y = 2x + 4$	
6	$2(1) + 4$
	6
LS = RS ✓	

$3x + y = 9$	
$3(1) + 6$	9
9	9
LS = RS ✓	

\therefore The solution is (1, 6)

Example 2

Solve the linear system using the method of substitution.

- ① $2y - 4x = 2$
- ② $y = -x + 4$

Sub ② into ①

$$\text{① } 2y - 4x = 2$$

$$\text{② } y = -x + 4$$

$$2(-x + 4) - 4x = 2$$

$$-2x + 8 - 4x = 2$$

$$8 - 6x = 2$$

$$-6x = -6$$

$$x = 1$$

Sub "1" for "x" in equation ②

$$y = -(1) + 4$$

$$y = 3$$

\therefore P.O.I. (solution) is (1, 3)

CHECK (1,3)	
$2y - 4x = 2$	
$2(3) - 4(1)$	2
6 - 4	2
2	2
LS = RS	

$y = -x + 4$	
3	$-(1) + 4$
3	3
LS = RS	

\therefore (1, 3) is the solution

① Subbing

② Solving for "x"

③ Solving for "y"

Example 3

Solve the linear system using the method of substitution.

- ① $2x + y = 7$
- ② $x - y = -1$

1) Rearrange ② into $y = mx + b$

$$x - y = -1$$

$$\frac{-y}{-1} = \frac{-x - 1}{-1}$$

$$\boxed{y = x + 1}$$

① $2x + y = 7$
② $y = x + 1$

sub ② in ①

$$2x + (x + 1) = 7$$

$$3x + 1 = 7$$

$$\frac{3x}{3} = \frac{6}{3}$$

$$\boxed{x = 2}$$

sub "2" for "x" in equation ②

$$y = x + 1$$

$$= 2 + 1$$

$$\boxed{y = 3}$$

\therefore PoI is (2, 3)

CHECK
(2, 3)

$2x + y$	7
$2(2) + 3$	7
$= 4 + 3$	7
$= 7$	7

LS = RS ✓

$x - y$	-1
$2 - 3$	-1
-1	-1

LS = RS ✓

\therefore The solution is (2, 3)

Example 4

Solve the linear system using the method of substitution.

- ① $2x - y = 4$
- ② $4x + y = 9$

i) Rearrange ① into $y = mx + b$

$$2x - y = 4$$

$$\frac{-y}{-1} = \frac{-2x + 4}{-1}$$

$$\boxed{y = 2x - 4}$$

① $y = 2x - 4$
② $4x + y = 9$

sub ① → ②

$$4x + (2x - 4) = 9$$

$$6x - 4 = 9$$

$$\frac{6x}{6} = \frac{13}{6}$$

$$\boxed{x = \frac{13}{6}}$$

sub " $\frac{13}{6}$ " for "x"

$$\textcircled{1} y = 2x - 4$$

$$= 2 \cdot \left(\frac{13}{6}\right) - 4$$

$$= \frac{13}{3} - \frac{4 \cdot 3}{1 \cdot 3}$$

$$= \frac{13}{3} - \frac{12}{3}$$

$$= \frac{13 - 12}{3}$$

$$\boxed{y = \frac{1}{3}}$$

\therefore PoI is $\left(\frac{13}{6}, \frac{1}{3}\right)$

CHECK
 $\left(\frac{13}{6}, \frac{1}{3}\right)$

y	$2x - 4$
$\frac{1}{3}$	$2\left(\frac{13}{6}\right) - 4$
	$\frac{13}{3} - 4$
	$\frac{1}{3}$

LS = RS ✓

$4x + y$	9
$4\left(\frac{13}{6}\right) + \frac{1}{3}$	9
$\frac{26}{3} + \frac{1}{3}$	
$\frac{27}{3}$	9

LS = RS ✓

\therefore The solution is $\left(\frac{13}{6}, \frac{1}{3}\right)$

PRACTICE

<p>1. ① $y = 2x + 1$ ② $y = -3x - 11$</p> $2x + 1 = -3x - 11$ $5x + 1 = -11$ $\frac{5x}{5} = \frac{-12}{5}$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$x = -\frac{12}{5}$</div> $y = 2x + 1$ $= 2\left(-\frac{12}{5}\right) + 1$ $= \frac{-24}{5} + \frac{1 \cdot 5}{1 \cdot 5}$ $= \frac{-24 + 5}{5}$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$y = -\frac{19}{5}$</div> <p>$\therefore \left(-\frac{12}{5}, -\frac{19}{5}\right)$</p>	<p>2. ① $y = 5x - 2$ ② $6x + 3y = 36$</p> <p>① \rightarrow ②</p> $6x + 3(5x - 2) = 36$ $6x + 15x - 6 = 36$ $21x - 6 = 36$ $21x = 42$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$x = 2$</div> $y = 5x - 2$ $= 5(2) - 2$ $= 10 - 2$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$y = 8$</div> <p>\therefore POI is $(2, 8)$</p>
<p>3. ① $2x + y = 3$ ② $-3x + y = -7$</p> <p>Rearrange ① into $y = mx + b$</p> <p>① $y = -2x + 3$ ② $-3x + y = -7$</p> $-3x + (-2x + 3) = -7$ $-3x - 2x + 3 = -7$ $-5x + 3 = -7$ $-5x = -10$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$x = 2$</div> $y = -2x + 3$ $y = -2(2) + 3$ $y = -4 + 3$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$y = -1$</div> <p>\therefore POI is $(2, -1)$</p>	<p>4. $2x + y = -1 \rightarrow y = -2x - 1$ $x - 13y = 13$</p> $x - 13(-2x - 1) = 13$ $x + 26x + 13 = 13$ $27x + 13 = 13$ $27x = 0$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$x = 0$</div> $y = -2(0) - 1$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$y = -1$</div> <p>\therefore POI is $(0, -1)$</p>
<p>Need to rearrange for $x =$ and substitute x first instead of y.</p>	
<p>5. $2x + 5y = -18 \rightarrow 2x + 5y = -18$ $x + 2y = -6 \rightarrow x = -2y - 6$</p> $2(-2y - 6) + 5y = -18$ $-4y - 12 + 5y = -18$ $-12 + y = -18$ $y = -6$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$y = -6$</div> $x = -2(-6) - 6$ $= 12 - 6$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">$x = 6$</div> <p>\therefore POI is $(6, -6)$</p>	
<p>ANSWERS: 1. $(-\frac{12}{5}, -\frac{19}{5})$, 2. $(2, 8)$, 3. $(2, -1)$, 4. $(0, -1)$, 5. $(6, -6)$</p>	